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## Article

# Coordinated Voltage Regulation Methods in Active Distribution Networks with Soft Open Points

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**Abstract:** This paper proposes a coordinated voltage regulation method for active distribution networks (ADNs) to mitigate nodal voltage fluctuations caused by photovoltaic (PV) power fluctuations, where a three-stage optimization scheme is developed to coordinate and optimize the tap position of on-load tap changers (OLTCs), the reactive power of capacitor banks (CBs), and the active and reactive power of soft open points (SOPs). The first stage aims to schedule the OLTC and CBs hourly using the rolling optimization algorithm. In the second stage, a multi-objective optimization model of SOPs is established to periodically (15 min) optimize the active and reactive power of each SOP. Meanwhile, this model is also responsible for optimizing the Q-V droop control parameters of each SOP used in the third stage. The aim of the third stage is to suppress real-time (1 min) voltage fluctuations caused by rapid changes in PV power, where the Q-V droop control is developed to regulate the actual reactive power of SOPs automatically, according to the measured voltage at the SOPs' connection points. Furthermore, numerous simulations and comparisons are carried out on a modified IEEE 33-bus distribution network to verify the effectiveness and correctness of the proposed voltage regulation method.

**Keywords:** active distribution network (ADN); voltage regulation; photovoltaic (PV); soft open point (SOP); droop control

## 1. Introduction

In recent years, environment protection and sustainability have become the main concern across the whole world. As is known to all, the access of distributed generations (DGs), such as photovoltaic (PV) plants and wind turbines, can reduce environmental pollution and energy crisis, and the application of PV power systems is particularly important for the sustainable development of the environment. Recently, a large number of PV plants have been connected to low-voltage distribution networks [1–3], but their output power has strong uncertainty and randomness, resulting in significant nodal voltage variations [4–6]. With the increase of PV penetrations, the bus voltage of distribution networks may frequently violate the voltage constraints defined by utility grids, which will damage the voltage stability and power quality of active distribution networks (ADNs) [7]. Thus, studying the voltage regulation methods of ADNs is of great significance to the operating, scheduling, and planning of distribution networks.

Traditional voltage regulation measures include switching on/off capacitor banks (CBs) and changing the tap position of on-load tap changers (OLTCs) [8]. However, the disadvantages are that they not only need too much time to respond to the control commands, but also their lifetimes are

limited [9], thus it is better to adjust their operating status as few times as possible. Clearly, using OLTCs and CBs is hard to fully solve the voltage issues of ADNs caused by active power fluctuations of high levels of PV. Therefore, to solve this problem, the active power of PV plants can be reduced to avoid bus voltages exceeding upper voltage constraints, but it will reduce the revenue of selling solar power [10,11]. Nowadays, using the rest capacity of PV converters to generate or absorb reactive power is a popular way for PV plants to participate in voltage regulation of ADNs [12,13]. However, it is difficult to centrally coordinate various PV plants due to their different ownership and the shortage of communication links between them. Furthermore, the usage of static var compensators, energy storage systems, and demand side response are also effective ways for regulating voltage variations [14–16]. However, unlike transmission systems, distribution networks have a large value of  $R/X$ , so that the voltage problem caused by power variations of large-scale PV plants cannot be effectively solved only by optimizing the reactive power distribution [17–19]. Therefore, the optimization of active and reactive power distribution of ADNs should be considered simultaneously to make full use of the advantages of various voltage control methods and devices, achieving a better voltage regulation result.

Recently, the technology of soft open points (SOPs) provides a new solution for voltage regulation of ADNs [20–22]. The SOP is a type of fully controlled power electronic devices, which can replace the tie switch in the traditional distribution network, and can significantly improve the flexibility and reliability of the system. Also, the greatest feature of the SOP is that the active and reactive power of its two sides can be controlled continuously and accurately. SOPs just need to ensure the active power balance, but they do not require that the reactive power outputs of two sides are the same [23–25]. For example, when one side of a SOP is absorbing reactive power, the other side can be controlled to generate or absorb reactive power.

Consequently, the active and reactive power profiles are optimized in [21] with the aim of minimizing total losses and bus voltage deviations of ADNs. Reference [24] mainly focuses on the coordination between SOPs and conventional tie switches, where the bus voltages can be mitigated within a certain range by the proposed bi-level model. References [26,27] allocate SOPs and DG units with or without network reconfiguration to optimize the voltage deviation index and load balancing index. In [28], a coordinated voltage and var control method based on SOPs and multiple regulation devices, such as the OLTC and CBs, is proposed, but all voltage control devices are optimized on the same time scale. As a result, this method has failed to fully utilize the fast voltage regulation capability of the SOPs. The above voltage regulation methods are centralized voltage control schemes, and the communication delays and a huge amount of calculations will significantly affect the voltage regulation results. In addition, the decentralized voltage control strategies based on SOPs can also be used to regulate the voltage variations in ADNs [29,30], but they neglect the uncertainties of renewable energy power outputs and loads during the optimization. The above methods can effectively control the voltage variations with a long-term timescale ( $\geq 15$  min), but these methods have not fully discussed the schemes and strategies of mitigating the voltage variations under smaller timescales (e.g., 10 s, 1 min).

However, to the best of our knowledge, the methods of using SOPs to control voltage variations of ADNs have not been fully investigated, and further studies are required to improve the previous studies on the coordinated control schemes of SOPs and traditional voltage control devices. Hence, this paper aims to develop an optimal control method of SOPs, OLTCs, and CBs for limiting nodal voltage fluctuations of ADNs caused by PV power fluctuations, ensuring that the distribution network has smaller losses, and the OLTCs and CBs have longer lifetime. The main contributions of this study are the following:

- (1) To minimize the bus voltage variations and operating losses of ADNs, a coordinated voltage control method for ADNs is developed, where the OLTC's tap position, the reactive power of CBs, and the active and reactive power of SOPs are coordinated and optimized via a three-stage optimization scheme.

(2) Based on the rolling optimization algorithm, a mixed-integer nonlinear optimization model is established to hourly optimize the tap position of OLTC and the numbers of capacitors switched on each CB, where the uncertainties of PV outputs and load demands are fully considered.

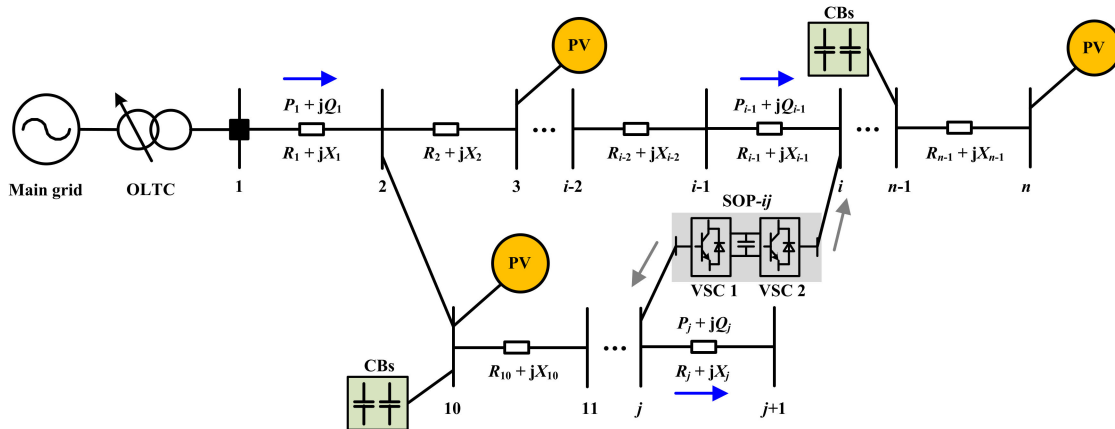
(3) A multi-objective optimization model of SOPs aiming at reducing voltage variations and operating losses of ADNs is established to periodically optimize the short-term active power and reactive reference power of each SOP. A Q-V droop control algorithm for SOPs is developed to regulate the actual reactive power compensation of each SOP, according to the local bus voltage.

(4) Several simulations and comparisons are carried out on a modified IEEE 33-bus distribution system using the real data of PV plants to prove the effectiveness of the proposed voltage regulation method.

The rest of this paper is organized as follows: Section 2 describes the system structure of an ADN including SOPs. The proposed voltage regulation method is presented in Section 3, including the overall control scheme, objective functions, decision variables, constraints, and solution methods. Case studies and discussions are presented in Section 4, and the conclusions of this work are summarized in Section 5.

## 2. System Description

Figure 1 presents the system topology of an ADN, including an OLTC, SOPs, PV plants, and CBs. The SOP is a power electronic device, which is used to replace the traditional tie switch in distribution networks, and it can achieve precise power control between two feeders. Various structures of SOPs are presented in [23], including back to back voltage source converters (B2B VSC), the unified power flow controller (UPFC), and the static synchronous series compensator (SSSC). This paper takes the B2B VSC as an example to investigate the coordinated voltage regulation methods of ADNs. The B2B VSC consists of two VSC converters, i.e., SOP- $ij$  shown in Figure 1. Also, the SOP has stronger power regulation ability and faster response speed compared with conventional voltage regulation devices. Different from the mechanical voltage regulation devices such as OLTCs, the SOP is a fully controlled power electronic converter and can quite quickly regulate its outputs of two sides [23,24,31]. In addition, the SOP can play a critical role in fault isolation and power restoration, because the fault current can be limited by the converters on both sides of the SOP, due to the isolation of the DC link [25].



**Figure 1.** System topology of an active distribution network (ADN) including the soft open point (SOP).

In this study, the total number of buses, branches, and CBs in the ADN are  $N$ ,  $L$ , and  $H$ , respectively.  $i$  and  $j$  are the index of buses (nodes),  $i, j \in \Phi_{\text{node}} = \{1, 2, \dots, N\}$ .  $l$  is the index of branches,  $l \in \Phi_{\text{bran}} = \{1, 2, \dots, L\}$ .  $R_l + jX_l$  is the impedance of branch  $l$ , and  $V_i$  denotes the voltage of bus  $i$ . The set  $V_{\text{node}}$  consists of the voltage of all buses,  $V_i \in V_{\text{node}}$ .  $I_{\text{bran}}$  is a set of the current of all branches,  $I_{\text{bran}} = \{I_1, I_2, \dots, I_l\}$ .  $S_o$  denotes the tap position of the OLTC, and  $S_{c,i}$  is the number of capacitors that are switched on CB  $i$ . The set  $S_C = \{S_{c,1}, S_{c,2}, \dots, S_{c,H}\}$ . The active and reactive power of the  $i$  side ( $j$  side) of SOP- $ij$  are denoted by  $P_{\text{SOP},i}^{ij}$  and  $Q_{\text{SOP},i}^{ij}$  ( $P_{\text{SOP},j}^{ij}$  and  $Q_{\text{SOP},j}^{ij}$ ), respectively. The sets  $P_S$  and  $Q_S$  consist of active

and reactive power of all SOPs, i.e.,  $P_{SOP,i}^{ij}, P_{SOP,j}^{ij} \in P_S$ , and  $Q_{SOP,i}^{ij}, Q_{SOP,j}^{ij} \in Q_S$ . The demand at bus  $i$  is  $P_{load,i} + jQ_{load,i}$ , and the active power injection of PV at bus  $i$  is  $P_{PV,i}$ , whereas the reactive power output of CB  $i$  is denoted by  $Q_{CB,i}$ . Also,  $t$  denotes the current time.

As can be seen from Figure 1, the output power fluctuations of a PV plant not only lead to voltage violations where the PV plant is connected to but also affect the voltage of other buses at the same feeder. When numerous PV plants installed in this ADN, the power quality will be extremely terrible if without any effective control ways. For example, sometimes, the bus voltage exceeds the upper voltage limit if the PV power is larger than loads, and sometimes the voltage may suddenly drop due to the rapid decline in PV power. Therefore, this study develops a voltage control method to avoid the above-discussed voltage issues.

### 3. Coordinated Voltage Regulation Methods

This section first gives the overall idea of the proposed voltage regulation methods, discusses the objective functions and decision variables of each stage, and explains the coordination relationships between each control stage. Then, the specific mathematical models and solution methods of this voltage control method are described, respectively.

#### 3.1. Overall Idea of the Proposed Voltage Regulation Methods

In this study, a coordinated control method of the OLTC, CBs, and SOPs is proposed to limit the nodal voltage variations of ADNs, which is achieved by optimizing the OLTC tap position, the reactive power compensation of CBs, and the active and reactive power output of SOPs. Therefore, the optimization described above is divided into three stages, as shown in Figure 2.

##### 3.1.1. First Stage (Long-Term Optimization)

In the first stage, an optimization model of the OLTC and CBs is established based on the rolling optimization algorithm, which mainly focuses on optimizing the tap position of the OLTC and the reactive power output of each CB. Thus, the long-term bus voltage variations caused by periodical changes of PV outputs and loads can be reduced. To reduce the number of changes of OLTCs and CBs, the optimization is implemented every 1 h according to the long-term predicted power of PV plants and loads.

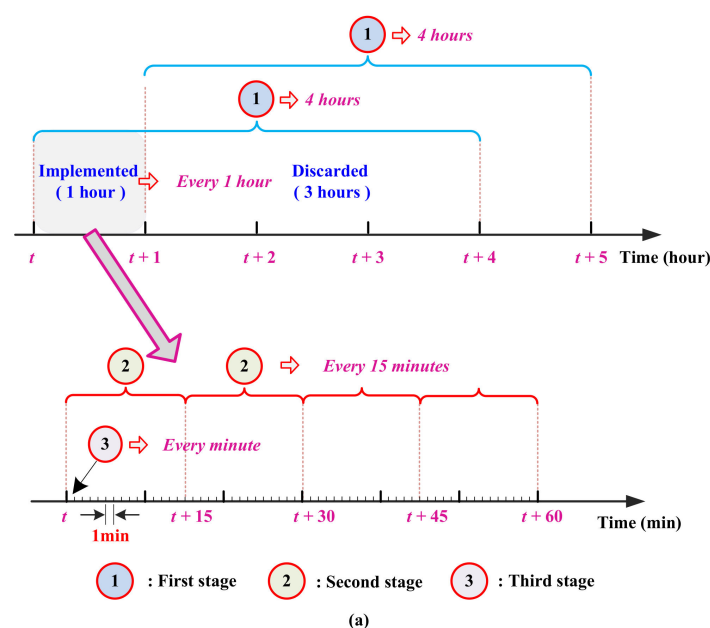
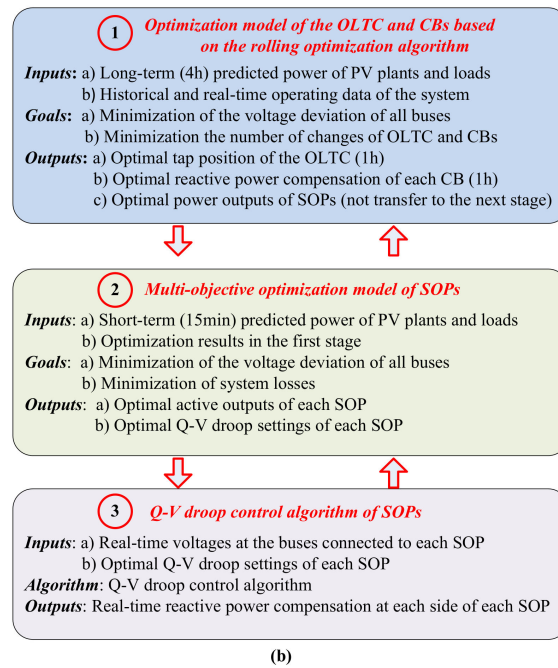


Figure 2. Cont.



**Figure 2.** Overall ideas of the proposed voltage regulation method: (a) The timescale of each stage; (b) input parameters, objective functions, and decision variables of each stage.

In summary, the objective function of the first stage is to minimize the voltage deviations and the number of changes of the OLTC and CBs. The decision variables consist of the OLTC tap position ( $S_o$ ), the number of capacitors switched on each CB ( $S_{c,i}$ ), and the active and reactive power of each SOP ( $P_{SOP,i}^{ij}$ ,  $Q_{SOP,i}^{ij}$ ,  $P_{SOP,j}^{ij}$  and  $Q_{SOP,j}^{ij}$ ). In this stage, SOPs are involved in the optimization process, but the optimization results of SOPs are not sent to the next stage. The actual outputs of SOPs are determined by the control method proposed in the second stage and third stage.

### 3.1.2. Second Stage (Short-Term Optimization)

The first stage determines the operating status of the OLTC and CBs in the next 1 h, hence the second stage aims to regularly optimize the running condition of all SOPs during the next 15 min. Therefore, a multi-objective optimization model of SOPs is established, and the model is executed every 15 min to achieve the following two goals:

- (1) To optimize the active power injection by each SOP.
- (2) To optimize the Q-V droop coefficients at each side of all SOPs. The Q-V droop control used in the third stage is to dynamically adjust the reactive power of SOPs, according to the real-time local bus voltage and the droop settings.

In summary, the objective function of the second stage is to minimize total bus voltage deviations and system losses, while the decision variables of the second stage are active power of SOPs ( $P_{SOP,i}^{ij}$  and  $P_{SOP,j}^{ij}$ ), reference reactive power of SOPs ( $Q_{SOP,i}^{ref,ij}$  and  $Q_{SOP,j}^{ref,ij}$ ), and the Q-V droop settings of SOPs. Eventually, the optimization results will be sent to the third stage.

### 3.1.3. Third Stage (Real-Time Control)

The third stage is executed every minute to mitigate the real-time nodal voltage variations. The Q-V droop control strategy is used for all SOPs to control the real-time reactive outputs in both sides of them. Namely, a SOP will automatically adjust its reactive power compensation based on the updated Q-V droop settings and the sampled voltage at the bus connected to the SOP.

In addition to the final reactive power outputs of SOPs, the remaining control variables just follow the control commands generated in the above two stages.



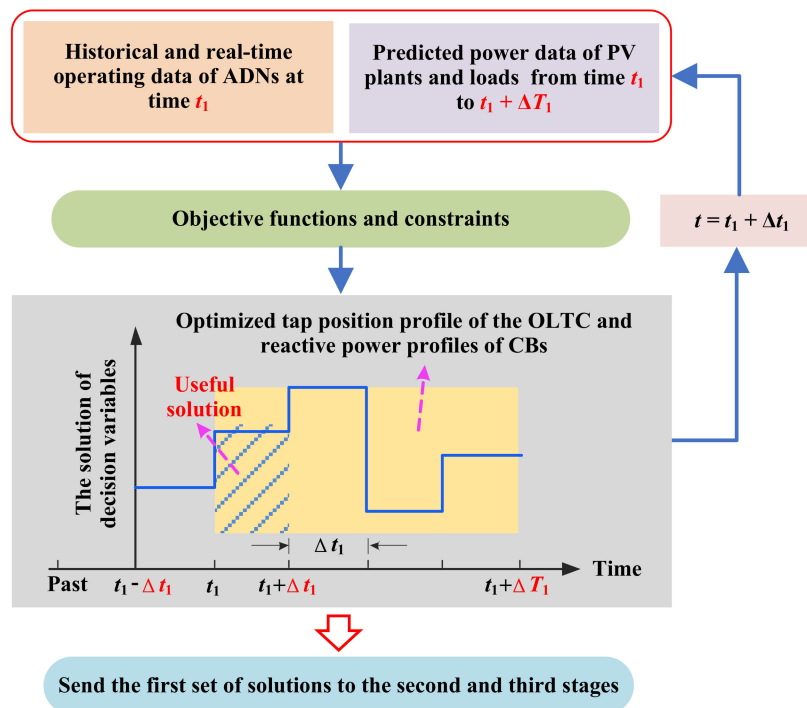
As explained above, the proposed voltage control method can make sure that the nodal voltage variations can be reduced as much as possible, through the coordination between these three stages. Their specific mathematical models are described in the following sections.

### 3.2. Optimization Models of the OLTC and CBs

This section discusses how to use the rolling optimization algorithm to determine the tap position of an OLTC and the reactive outputs of CBs. Hence, this section begins by describing the rolling optimization framework and goes on to discuss mathematical expressions of the established models.

#### 3.2.1. Rolling Optimization Framework

In order to account for the uncertainties of PV outputs and loads, a rolling optimization is developed, which is shown in Figure 3 [32,33]. First, some advanced prediction techniques are utilized to predict the output power of all PV plants and the load power from time  $t_1$  to  $t_1 + \Delta T_1$ , where  $\Delta T_1$  is the total prediction time, e.g., 4 h in this study, and the predicted time interval  $\Delta t_1$  is 1 h in this study. Then, taking the predicted data and the current operation data of ADNs as the input, the objective function will be minimized to gain the optimal profiles of the OLTC's tap position and the reactive outputs of CBs from time  $t_1$  to  $t_1 + \Delta T_1$ . However, only the optimization results of the first hour (i.e., from time  $t_1$  to  $t_1 + \Delta t_1$ ) are adopted, and the remaining optimization results (i.e., from time  $t_1 + \Delta t_1$  to  $t_1 + \Delta T_1$ ) are neglected.



**Figure 3.** Principle of optimizing the on-load tap changer's (OLTCs) tap position and capacitor banks' (CBs') reactive outputs using the rolling optimization algorithm.

Finally, the above optimization will be executed again at  $t_1 + \Delta t_1$ , and the predicted data of PV plants and loads will be updated. Hence, we can get more accurate and effective optimization results, compared with the cases where all optimal solutions were adopted.

#### 3.2.2. Mathematical Models

The objective function of the established optimization model,  $f_1$ , aims at minimizing the total voltage deviations of all nodes and the number of changes of OLTC and CBs, as follows:

Objective function:

$$\min f_1(S_o, S_C, P_S, Q_S) = \sum_{t=t_1}^{t_1+\Delta T_1} (\rho_1 U_{\text{dev}}(t) + \rho_2 (F_{\text{CB}}(t) + F_{\text{OLTC}}(t))) \quad (1)$$

$$U_{\text{dev}}(t) = \sum_{i \in \Phi_{\text{node}}} (|V_i(t)^2 - V_L^2| + |V_i(t)^2 - V_U^2|) \quad (2)$$

$$F_{\text{CB}}(t) = \sum_{i \in \Phi_{\text{node}}} |S_{c,i}(t) - S_{c,i}(t - \Delta t_1)| \quad (3)$$

$$F_{\text{OLTC}}(t) = |S_o(t) - S_o(t - \Delta t_1)| \quad (4)$$

where  $S_o$ ,  $S_C$ ,  $P_S$ , and  $Q_S$  are decision variables. Function  $U_{\text{dev}}$  denotes the voltage variation of all nodes in the ADN, and functions  $F_{\text{CB}}$  and  $F_{\text{OLTC}}$  denote the changing times of the OLTC and CBs during the current optimization period, respectively.  $\rho_1$  and  $\rho_2$  are weight coefficients and are utilized to represent the importance of the sub-objective functions, and  $\rho_1 + \rho_2 = 1$ . The larger value of  $\rho_1$  is, the more important the sub-objective function  $U_{\text{dev}}$  is. Since the minimization of nodal voltage variations is the primary concern of voltage regulation for ADNs, the sub-objective function  $U_{\text{dev}}$  is more important than functions  $F_{\text{CB}}$  and  $F_{\text{OLTC}}$  in the objective function  $f_1$ . The analytic hierarchy process (AHP) [28] has been widely used in complex decision-making problems, which can determine the weight coefficients of sub-objective functions in terms of the importance of them. Therefore, this paper uses the AHP to determine the values of  $\rho_1$  and  $\rho_2$ , and this paper sets  $\rho_1 = 0.87$ ,  $\rho_2 = 0.13$ .  $V_L$  and  $V_U$  are ideal voltage variation limits, e.g.,  $V_L = 0.98$  p.u. and  $V_U = 1.02$  p.u. [29].

Constraints:

The model should meet the power flow constraints, as follows. (5)–(10) are power flow constraints, where (5) and (6) are active and reactive power balance equations; (11) is the bus voltage limit, and (12) denotes the branch current limit. (13)–(18) are the operating requirements of the OLTC and CBs, respectively. Moreover, the constraints of SOPs are described by (19)–(23), where the active power balance of a SOP is described in (19)–(21), and the reactive power limit at each side of a SOP is described in (22). Also, (23) requires that the total active and reactive output at each side of a SOP should be less than its capacity.

$$\sum_{jk \in \Phi_{\text{bran}}} P_{jk}(t) - \sum_{ij \in \Phi_{\text{bran}}} (P_{ij}(t) - R_{ij} I_{ij}(t)^2) = P_i(t) \quad (5)$$

$$\sum_{jk \in \Phi_{\text{bran}}} Q_{jk}(t) - \sum_{ij \in \Phi_{\text{bran}}} (Q_{ij}(t) - X_{ij} I_{ij}(t)^2) = Q_i(t) \quad (6)$$

$$V_i(t)^2 - V_j(t)^2 + (R_{ij}^2 + X_{ij}^2) I_{ij}(t)^2 = 2(R_{ij} P_{ij}(t) + X_{ij} Q_{ij}(t)) \quad (7)$$

$$V_i(t)^2 I_{ij}(t)^2 = P_{ij}^2(t) + Q_{ij}^2(t) \quad (8)$$

$$P_i(t) = P_{\text{PV},i}(t) + P_{\text{SOP},i}^{ij}(t) - P_{\text{load},i}(t) \quad (9)$$

$$Q_i(t) = Q_{\text{PV},i}(t) + Q_{\text{SOP},i}^{ij}(t) - Q_{\text{load},i}(t) \quad (10)$$

$$V_{\min}^2 \leq V_i(t)^2 \leq V_{\max}^2 \quad (11)$$

$$I_l(t)^2 \leq I_{l,\max}^2 \quad (12)$$

$$S_o^{\min} \leq S_o(t) \leq S_o^{\max}, S_o(t) \in \mathbb{Z} \quad (13)$$

$$\sum_{t=t_1}^{t_1+\Delta T_1} |S_{c,i}(t) - S_{c,i}(t - \Delta t_1)| \leq \gamma_{c,\max} \quad (14)$$



$$Q_i^{CB}(t) = \Delta Q_{c,i} \times S_{c,i}(t) \quad (15)$$

$$\sum_{t=t_1}^{t_1+\Delta T_1} |S_o(t) - S_o(t - \Delta t_1)| \leq \gamma_{o,\max} \quad (16)$$

$$0 \leq S_{c,i}(t) \leq S_{c,i}^{\max}, S_{c,i}(t) \in \mathbb{N} \quad (17)$$

$$V_i(t) = 1.0 + \Delta U_o \times S_o(t) \quad (18)$$

$$P_{SOP,i}^{ij}(t) + P_{SOP,j}^{ij}(t) + P_{SOP,i}^{ij,loss}(t) + P_{SOP,j}^{ij,loss}(t) = 0 \quad (19)$$

$$P_{SOP,i}^{ij,loss}(t) = \mu \sqrt{P_{SOP,i}^{ij}(t)^2 + Q_{SOP,i}^{ij}(t)^2} \quad (20)$$

$$P_{SOP,j}^{ij,loss}(t) = \mu \sqrt{P_{SOP,j}^{ij}(t)^2 + Q_{SOP,j}^{ij}(t)^2} \quad (21)$$

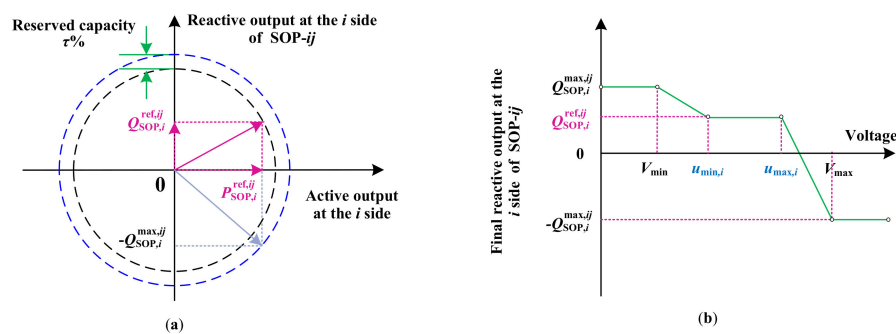
$$Q_{SOP}^{\min,ij} \leq Q_{SOP,i}^{ij}(t), Q_{SOP,j}^{ij}(t) \leq Q_{SOP}^{\max,ij} \quad (22)$$

$$\begin{cases} \sqrt{P_{SOP,i}^{ij}(t)^2 + Q_{SOP,i}^{ij}(t)^2} \leq C_{SOP}^{ij} \\ \sqrt{P_{SOP,j}^{ij}(t)^2 + Q_{SOP,j}^{ij}(t)^2} \leq C_{SOP}^{ij} \end{cases} \quad (23)$$

where  $P_{ij}$  and  $Q_{ij}$  are active and reactive power flows of branch  $ij$ ;  $P_i$  and  $Q_i$  are active and reactive power injections at bus  $i$ , respectively;  $R_{ij}$  and  $X_{ij}$  are resistance and reactance of branch  $ij$ , respectively.  $V_1$  is the voltage of bus 1, and  $\Delta U_o$  is the voltage step of the OLTC.  $\Delta Q_{c,i}$  is the unit capacity of a capacitor in CB  $i$ . It is assumed that the statutory voltage range is  $[V_{\min}, V_{\max}]$ , e.g.,  $[0.95, 1.05]$  p.u. [28].  $I_{l,\max}$  is the maximum allowable current of branch  $l$ . The range of  $S_o$  is  $[S_o^{\min}, S_o^{\max}]$ , and the range of  $S_{c,i}$  is  $[0, S_{c,i}^{\max}]$ .  $\gamma_{o,\max}$  and  $\gamma_{c,\max}$  denote the maximum allowed adjustments of an OLTC and a CB during the current optimization period, respectively. Furthermore,  $P_{SOP,i}^{ij}$  ( $P_{SOP,j}^{ij}$ ),  $Q_{SOP,i}^{ij}$  ( $Q_{SOP,j}^{ij}$ ), and  $P_{SOP,i}^{ij,loss}$  ( $P_{SOP,j}^{ij,loss}$ ) denote the active power, reactive power and the active power loss at the  $i$  side ( $j$  side) of the SOP- $ij$ , respectively.  $C_{SOP}^{ij}$  is the rated capacity of SOP- $ij$ , and  $\mu$  is the loss coefficient of SOPs, i.e., a factor for evaluating the active power loss of SOPs [29–31].

### 3.3. Optimization Models of SOPs

In this section, as shown in Figure 4, the established multi-objective optimization model of SOPs will be executed twice using the known tap position of the OLTC, reactive outputs of all CBs, and the predicted power of all PV plants and loads during the period from time  $t$  to  $t + \Delta T_2$  ( $\Delta T_2 = 15$  min in this study).



**Figure 4.** Methods of optimizing the output power of SOPs: (a) Schematic diagram of optimizing the active and basic reactive power at the  $i$  side of SOP- $ij$ ; (b) schematic diagram of optimizing the Q-V droop coefficients at the  $i$  side of SOP- $ij$ .

(1) For the first time of executing this model, the active and basic reactive outputs of each SOP during the period from time  $t$  to  $t + \Delta T_2$  are determined, e.g., decision variables are  $P_{SOP,i}^{ref,ij}$  and  $Q_{SOP,i}^{ref,ij}$  for SOP- $ij$  at the  $i$  side, as shown in Figure 4a. However,  $P_{SOP,i}^{ref,ij}$  will be directly sent to the SOP- $ij$  as a control command, while  $Q_{SOP,i}^{ref,ij}$  will be regarded as the basic reactive power compensation at the  $i$  side of the SOP- $ij$ , as shown in Figure 4b. The final reactive outputs of SOPs will be determined by the droop control in the third stage. Furthermore, the capacities of SOPs are reserved  $\tau\%$  during this optimization, as shown in Figure 4a, and the reserved capacity will be used when optimizing the Q-V droop coefficients of each SOP.

(2) For the second time of executing this model,  $P_{SOP,i}^{ref,ij}$  and  $Q_{SOP,i}^{ref,ij}$  ( $\forall i, j \in \Phi_{node}$ ) are the known quantities. Thus, the decision variables are Q-V droop coefficients for each SOP, e.g.,  $u_{min,i}$  and  $u_{max,i}$  shown in Figure 4b. Note that  $Q_{SOP,i}^{max,ij}$  is related to the reserved capacity and the optimization results in the first optimization.

Therefore, the following section describes the mathematical expressions of the established multi-objective optimization model of SOPs in two steps.

### 3.3.1. Optimization of Active and Reactive Power of SOPs

The objective function of the established multi-objective optimization model,  $f_2$ , aims at minimizing the total voltage deviations of all nodes,  $U_{dev}$ , and the total operating losses of entire ADNs and all SOPs,  $P_{loss}$ , as follows:

$$\min f_2 = \rho_3 U_{dev}(t) + \rho_4 P_{loss}(t) \quad (24)$$

$$P_{loss}(t) = \sum_{l \in \Phi_{bran}} [(I_l(t))^2 R_l] + \sum_{i \in \Phi_{node}} P_{SOP,i}^{ij,loss}(t) \quad (25)$$

where  $P_{loss}$  is the active power loss of ADN and SOPs.  $\rho_3$  and  $\rho_4$  are weight coefficients. As explained in earlier, this paper utilizes the AHP to decide the values of  $\rho_3$  and  $\rho_4$ . Considering that the voltage has been controlled to a certain extent in the previous stage, this stage mainly focuses on the minimization of power losses of the system. Therefore, this paper sets  $\rho_3 = 0.3$ ,  $\rho_4 = 0.7$ .

In the first step, the decision variables are  $P_{SOP,i}^{ref,ij}(t)$ ,  $P_{SOP,j}^{ref,ij}(t)$ ,  $Q_{SOP,i}^{ref,ij}(t)$ , and  $Q_{SOP,j}^{ref,ij}(t)$ ,  $\forall i, j \in \Phi_{node}$  and  $i \neq j$ . Also, the constraints (5)–(12), and (19)–(23) are described in Section 3.2.2, where the variables  $P_{SOP,i}^{ij}$  and  $Q_{SOP,i}^{ij}$  should be replaced with  $P_{SOP,i}^{ref,ij}$  and  $Q_{SOP,i}^{ref,ij}$ , respectively; the loads and PV power at time  $t$  can be predicted using a short-term power prediction method. In addition to these constraints, the following constraint indicates the reserved SOP capacity:

$$\begin{cases} \sqrt{P_{SOP,i}^{ref,ij}(t)^2 + Q_{SOP,i}^{ref,ij}(t)^2} \leq (1 - \tau\%) C_{SOP}^{ij} \\ \sqrt{P_{SOP,j}^{ref,ij}(t)^2 + Q_{SOP,j}^{ref,ij}(t)^2} \leq (1 - \tau\%) C_{SOP}^{ij} \end{cases} \quad (26)$$

### 3.3.2. Optimization of Q-V Droop Coefficients of SOPs

In the second step, the objective function is optimized again based on the same power data of PV plants and loads as well as the optimization results obtained in the first step, but decision variables and some constraints are changed. Namely, decision variables are Q-V droop coefficients at the  $i$  and  $j$  sides of the SOP- $ij$ , i.e.,  $u_{min,i}(t)$ ,  $u_{max,i}(t)$ ,  $u_{min,j}(t)$ , and  $u_{max,j}(t)$ ,  $\forall i, j \in \Phi_{node}$  and  $i \neq j$ , as shown in Figure 4b. In addition to the constraints described in (5)–(12) and (19)–(22), the following constraints are added:

$$\begin{cases} Q_{SOP,i}^{max,ij}(t) = \sqrt{C_{SOP}^{ij}{}^2 - P_{SOP,i}^{ref,ij}(t)^2} \\ Q_{SOP,j}^{max,ij}(t) = \sqrt{C_{SOP}^{ij}{}^2 - P_{SOP,j}^{ref,ij}(t)^2} \end{cases} \quad (27)$$

$$\begin{cases} Q_{SOP,i}^{ij}(t) = g_i(V_i(t))Q_{SOP,i}^{\max,ij}(t) \\ Q_{SOP,j}^{ij}(t) = g_j(V_j(t))Q_{SOP,j}^{\max,ij}(t) \end{cases} \quad (28)$$

where  $Q_{SOP,i}^{\max,ij}$  and  $Q_{SOP,j}^{\max,ij}$  are the maximum allowed reactive power compensation at each side of SOP- $ij$ ; functions  $g_i$  and  $g_j$  can respectively find the reactive power compensation of SOP- $ij$  corresponding to the bus voltage  $V_i$  and  $V_j$  on the Q-V droop curves. Taking  $g_i(V_i(t))$  as an example, it can be calculated as follows:

$$g_i(V_i(t)) = \begin{cases} 1, & V_i(t) \leq V_{\min} \\ 1 + \frac{(1-\omega_i(t))(V_i(t)-V_{\min})}{V_{\min}-u_{\min,i}(t)}, & V_{\min} < V_i(t) < u_{\min,i}(t) \\ \omega_i(t), & u_{\min,i}(t) \leq V_i(t) \leq u_{\max,i}(t) \\ \frac{(\omega_i(t)+1)(V_i(t)-V_{\max})}{u_{\max,i}(t)-V_{\max}} - 1, & u_{\max,i}(t) < V_i(t) \leq V_{\max} \\ -1, & V_i(t) > V_{\max} \end{cases} \quad (29)$$

$$\omega_i(t) = Q_{SOP,i}^{\text{ref},ij}(t)/Q_{SOP,i}^{\max,ij}(t) \quad (30)$$

### 3.4. Q-V Droop Control of SOPs

As shown in Figure 5, at time  $t$ , each SOP automatically adjusts its reactive outputs at both sides according to the real-time bus voltages and the updated Q-V droop curves. For example, for the droop curve at the  $i$  side of SOP- $ij$ , if the real-time voltage at bus  $i$  is within a range of  $[u_{\min,i}, u_{\max,i}]$ , the final reactive output at the  $i$  side  $Q_{SOP,i}^{ij}$  is equal to  $Q_{SOP,i}^{\text{ref},ij}$ , which is determined in Section 3.3.1, otherwise, the final value of  $Q_{SOP,i}^{ij}$  is determined by the droop curve.

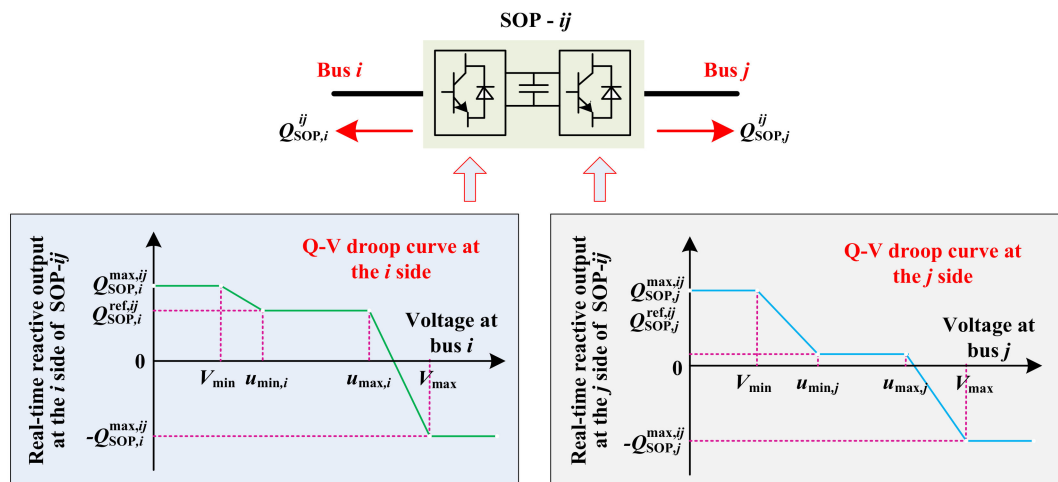


Figure 5. The Q-V droop control of a SOP.

### 3.5. Solution Algorithms of All Established Models

This section discusses the methods of solving the established optimization models. It can be seen that the model in the first stage is a mixed-integer nonlinear programming (MINLP) problem, and the model developed in the second stage is a nonlinear programming (NLP) problem. Meanwhile, they all contain quadratic constraints. To solve this problem, the original models are transformed into the mixed integer second-order cone programming (MISOCP) problem by conic relaxations.

#### 3.5.1. Conversion to an MISOCP Model

Therefore, this study converts these models into MISOCP model, where the objective functions and nonlinear constraints will be linearized. The MISOCP has been widely used in the planning and

operation optimization of distribution networks, because it can quickly and effectively solve nonlinear programming problems [28–31]. In this work, constraints that need to be converted are:

- (1) Power flow constraints: (5)–(12).
- (2) Operation constraints of OLTCs and CBs: (13)–(18).
- (3) SOP constraints: (19)–(23) and (26)–(27).
- (4) Constraints related to droop control of SOPs: (28)–(30).

Among the constraints listed above, in addition to the constraints (28)–(30), the conversion methods of the remaining constraints have been fully demonstrated and used. Thus, this study will not discuss them carefully, and their details can be found in [28]. Linearization of constraints (28)–(30) is performed by introducing auxiliary variables, as follows:

$$V_i(t) = 0.9\lambda_{i,1}(t) + V_{\min}\lambda_{i,2}(t) + u_{\min,i}(t)\lambda_{i,3}(t) + u_{\max,i}(t)\lambda_{i,4}(t) + V_{\max}\lambda_{i,5}(t) + 1.1\lambda_{i,6}(t) \quad (31)$$

$$g_i(V_i(t_2)) = \lambda_{i,1}(t_2) + \lambda_{i,2}(t_2) + \lambda_{i,3}(t_2)\omega_i(t_2) + \lambda_{i,4}(t_2)\omega_i(t_2) - \lambda_{i,5}(t_2) - \lambda_{i,6}(t_2) \quad (32)$$

where  $\lambda_{i,k}$  ( $k = 1, 2, \dots, 6$ ) is used to accurately describe the position corresponding to the current voltage on the droop curve, and the nonlinear part  $u_{\min,i}(t)\lambda_{i,3}(t)$  is linearized using auxiliary variables  $x_{i,d}$ ,  $\beta_{i,d}$ ,  $\eta_{i,d}$ , and  $M$ , as shown in (33)–(36).  $x_{i,d}$  and  $\eta_{i,d}$  are binary variables (i.e., 0–1 variables), and  $M$  is a large positive integer. Also,  $u_{\max,i}(t)\lambda_{i,4}(t)$  can be linearized using the same method.

$$u_{\min,i}(t)\lambda_{i,3}(t) = \left( 0.9 + 0.01 \sum_{d=0}^4 2^d x_{i,d}(t) \right) \lambda_{i,3}(t) \quad (33)$$

$$\beta_{i,3,d}(t) = x_{i,d}(t)\lambda_{i,3}(t) \quad (34)$$

$$\lambda_{i,3}(t) - M(1 - \eta_{i,3,d}(t)) \leq \beta_{i,3,d}(t) \leq \lambda_{i,3}(t) \quad (35)$$

$$0 \leq \beta_{i,3,d}(t) \leq M\eta_{i,3,d}(t) \quad (36)$$

In addition, to ensure that the reactive power compensation corresponding to the current voltage on the droop curve is unique, the following equations should be added:

$$\lambda_{i,1}(t) \leq s_{i,1}(t) \quad (37)$$

$$\lambda_{i,6}(t) \leq s_{i,5}(t) \quad (38)$$

$$\lambda_{i,k}(t) \leq s_{i,k}(t) + s_{i,k-1}(t), k = 2, 3, 4, 5 \quad (39)$$

$$\sum_{k=1}^6 \lambda_{i,k}(t) = 1 \quad (40)$$

$$\sum_{k=1}^5 s_{i,k}(t) = 1 \quad (41)$$

where  $s_{i,k}$  ( $k = 1, 2, \dots, 6$ ) are binary variables, representing five line segments in the droop curve, respectively, and they are adopted to limit the range of  $\lambda_{i,k}$  ( $k = 1, 2, \dots, 6$ ).

### 3.5.2. Calculation

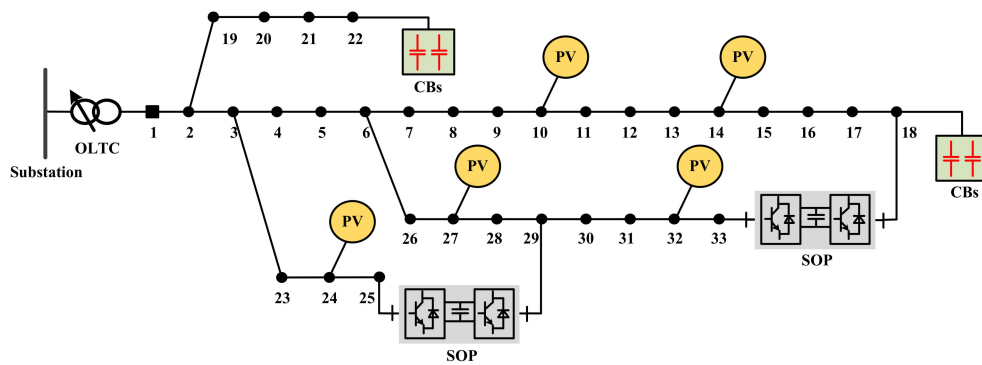
In this work, the MISOCP models are solved on the MATLAB@R2015b platform (2015 release, The MathWorks, Inc., Natick, MA, USA), where the decision variables, objective functions, and constraints are described using the YAMLP toolbox (R20190425, Johan Löfberg, Linköping University, Sweden), and the commercial solver IBM ILOG CPLEX (version 12.6, IBM Corporation, Armonk, NY, USA) [31] is utilized to find the best solution of the established optimization models. In addition,

all the simulations are conducted on a PC with Windows10 OS, Inter(R) Core i7 CPU @1.80 GHz, and 8.0 GB RAM.

## 4. Case Study

### 4.1. Simulation Parameters

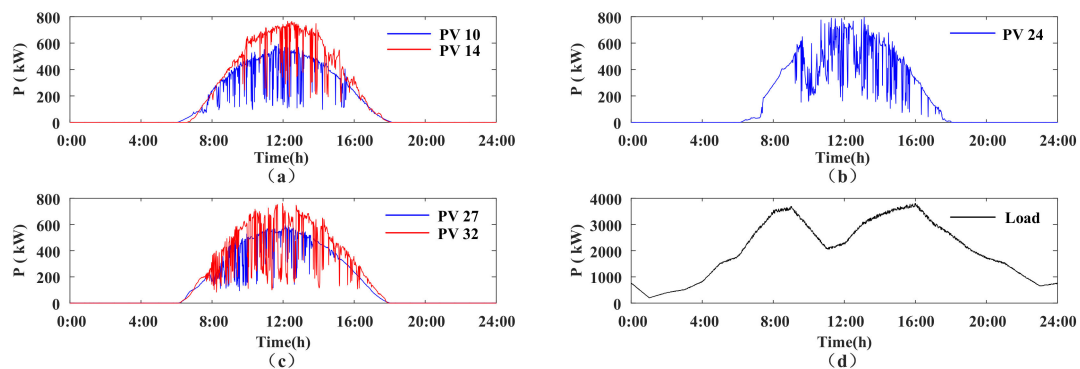
In this work, the proposed voltage regulation method is verified on a modified IEEE 33-bus radial distribution system, as shown in Figure 6. An OLTC is connected to bus 1, and its voltage regulation range is  $[0.95, 1.05]$  p.u. (0.005 p.u./step). CBs 1 and 2 are installed at buses 18 and 22, respectively. The total capacity of each CB is 300 kVar, including 5 capacitors. SOP 1 and SOP 2 are connected to buses 18 and 33, as well as buses 25 and 29, respectively. The capacity of each SOP is 800 kVA, and the loss coefficient is 0.02 [31]. The installed capacity and location of each PV plant is shown in Table 1. In addition, the daily power profiles of each PV plant are obtained from a real 750 kWp PV plant located in Sri Lanka [10], and the load power profile is obtained from [28], which is a typical daily power curve for industrial loads, as shown in Figure 7.



**Figure 6.** A modified IEEE 33-node system with an OLTC, photovoltaic (PV) plants, CBs and SOPs.

**Table 1.** Installed capacities and locations of PV plants.

PV Plants	Location	Rated Capacity (kVA)
PV 1	Bus 10	600
PV 2	Bus 14	800
PV 3	Bus 24	800
PV 4	Bus 27	600
PV 5	Bus 32	800

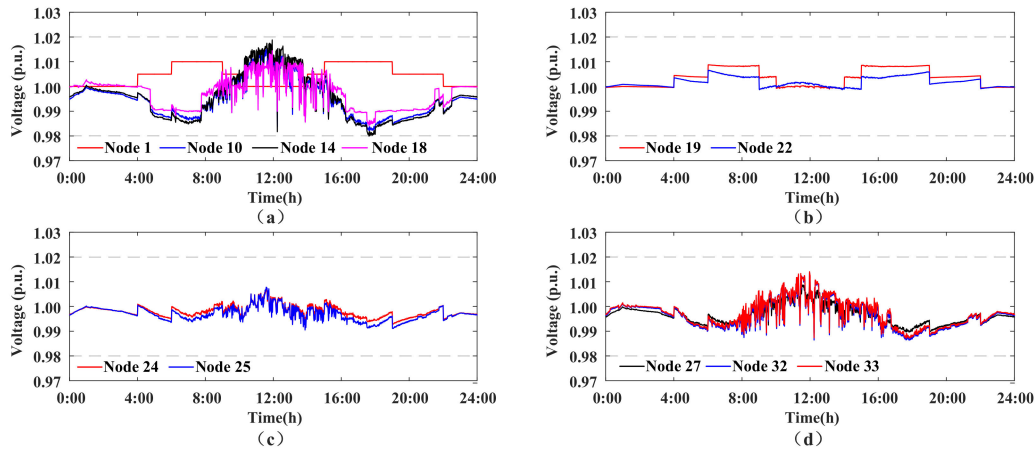


**Figure 7.** Daily power profiles of each PV plant and all loads: (a) PV plants connected to feeder1; (b) PV plants connected to feeder2; (c) PV plants connected to feeder3; (d) all loads.

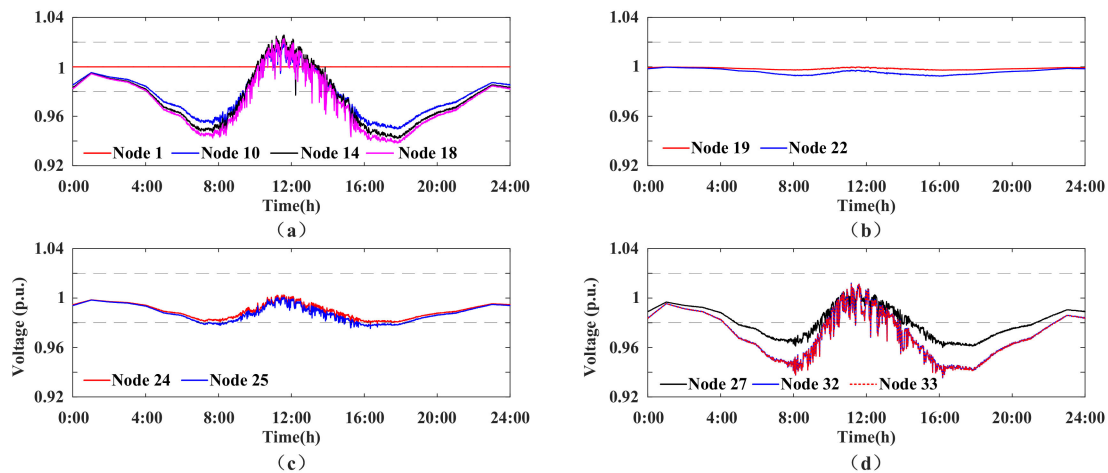
## 4.2. Simulation Results

### 4.2.1. Voltage Regulation Results

Based on the simulation cases described above, the voltage profiles after performing the proposed voltage regulation method are presented in Figure 8, and the voltage profiles without performing any voltage control scheme are shown in Figure 9.



**Figure 8.** Daily voltage profiles after performing the proposed voltage regulation method: (a) Feeder1; (b) Feeder2; (c) Feeder 3; (d) Feeder 4.



**Figure 9.** Daily voltage profiles before performing the proposed voltage regulation method: (a) Feeder1; (b) Feeder2; (c) Feeder 3; (d) Feeder 4.

Looking at Figure 8, the bus voltage fluctuations are within the ideal range, [0.9800, 1.0195], whereas the original voltage fluctuation range is [0.9352, 1.0260] (without optimization) in Figure 9, and the average bus voltage deviation is reduced from 1.7854 p.u. to 1.1588 p.u. They indicate that the proposed voltage control scheme can effectively mitigate bus voltage fluctuations caused by PV power variations. Furthermore, the total system loss is reduced from 1113.65 kWh to 594.98 kWh after optimization, indicating that the proposed voltage control method has a remarkable effect on reducing operating losses of distribution networks.

### 4.2.2. Optimization Results of the OLTC and CBs

After optimization, the optimal tap position of the OLTC and the reactive outputs of each SOP are shown in Figure 10, where the OLTC is adjusted 8 times a day, and the number of daily adjustments of



all CBs is 10 times. Furthermore, when the PV power generation is at a high level, the voltage at bus 1 is reduced by declining the OLTC's tap position. Meanwhile, the CBs correspondingly reduce their reactive outputs to avoid the bus voltage exceeding the upper voltage limit. These results show that the developed optimization model of the OLTC and CBs based on the rolling optimization algorithm can correctly regulate their operation status and reduce their changing times.

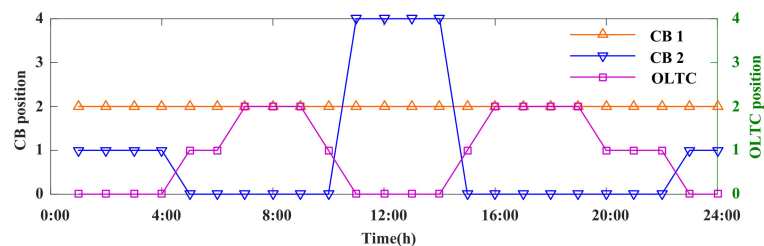


Figure 10. Optimal profile of the tap position of the OLTC and CBs.

#### 4.2.3. Optimal Active and Reactive Power Profiles of SOPs

After optimization, the real-time active and reactive outputs at each side of SOP are shown in Figure 11.

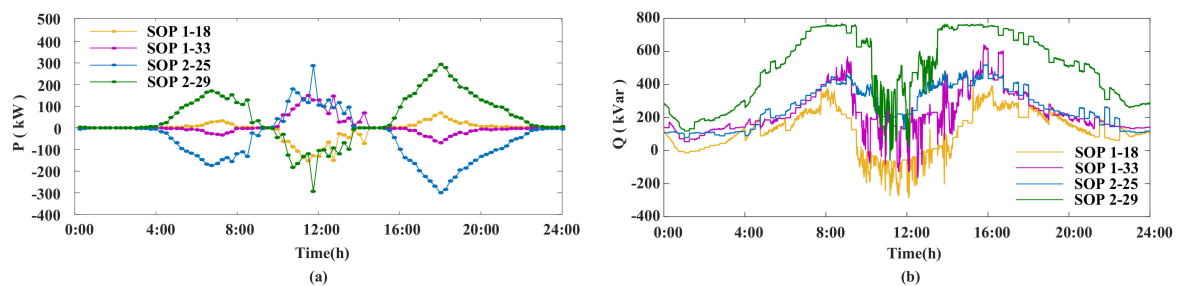
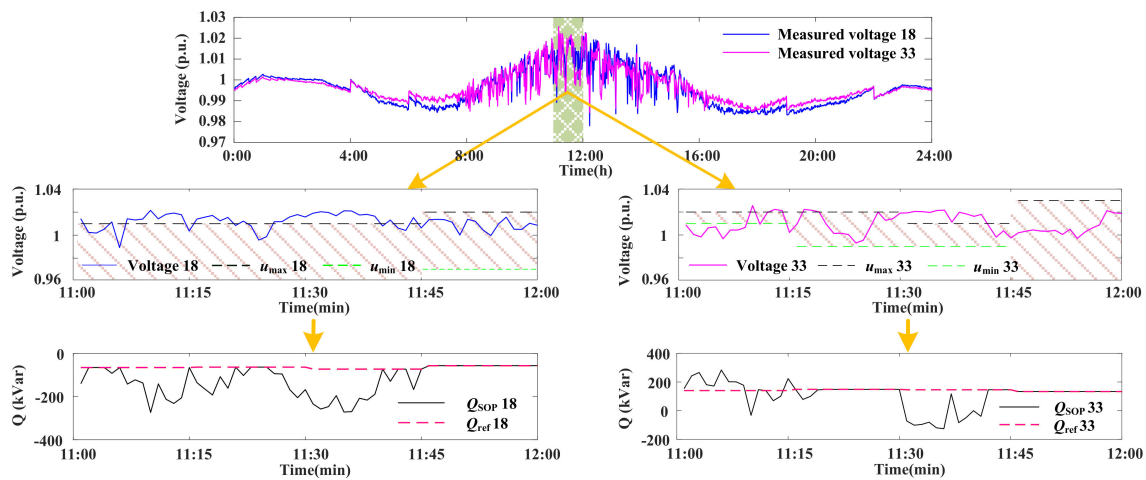


Figure 11. Daily power profiles of each SOP after optimization: (a) Active power; (b) reactive power.

As can be seen from Figure 11b, for any SOP, their reactive outputs of both sides are independent and can be regulated flexibly and separately. In summary, these results indicate that the established multi-objective optimization model of SOPs can properly allocate and coordinate the active outputs and reactive power compensation of all SOPs, ensuring that they can effectively respond to various bus voltage fluctuations.

As discussed earlier, the Q-V droop coefficients of each SOP are optimized after optimizing the active and reactive power of SOPs. Therefore, in order to further explain the relationship between the basic reactive power compensation and the final reactive outputs of SOPs, the following simulations discuss the reactive power regulation process of the SOP connected at bus 18 and 33. Figure 12 shows the optimized Q-V droop coefficients, initial bus voltages, and final reactive outputs of the SOP 18–33 from 11:00 to 12:00.

As can be seen from Figure 12, during 11:01–11:30, the dead zone of Q-V droop curve at bus 18 is  $[0.96, 1.01]$  p.u., and the basic reactive power compensation of the SOP is  $-65$  kVar. Hence, the final reactive power output is equal to  $-65$  kVar if the real-time voltage at bus 18 is within the dead zone,  $[0.96, 1.01]$ . However, sometimes the voltage at bus 18 exceeds the upper limit of the dead zone, thus the SOP correspondingly reduces its reactive output. Similarly, the SOP increases its reactive power output if the voltage at bus 33 is lower than the lower limit of the dead zone from 11:01 to 11:15. These results demonstrate that the proposed Q-V droop control strategy of SOPs can effectively regulate the reactive power compensation of each SOP to reduce the real-time bus voltage fluctuations.



**Figure 12.** Optimized Q-V droop coefficients, initial bus voltages, and final reactive outputs of the SOP 18–33 from 11:00 to 12:00.

#### 4.3. Comparisons of Different Voltage Regulation Methods

To analyze the advantages and disadvantages of the proposed voltage control methods, five methods are compared and analyzed under the same case. The reference voltage control methods are summarized as follows:

Method I: No voltage control scheme is conducted on ADNs, i.e., ADNs are operating without performing any voltage control scheme.

Method II: A combined voltage control method is proposed in [30], where only SOPs are utilized to regulate the voltage variations of ADNs.

Method III: This method is the combination of the method developed in [30] and the control scheme used in the first stage of the proposed voltage control.

Method IV: This method does not consider the optimization of Q-V droop settings of SOPs, and the remaining control process is the same as the method developed in this paper. Also, the Q-V droop settings of SOPs are set to the values used in [13].

Method V: The proposed voltage control method is conducted without the Q-V droop control of SOPs. Namely, the reactive power output of SOPs in the third stage is the fixed value after performing the second stage optimization.

Table 2 shows the optimization results of different voltage regulation methods. In addition, the minimum and maximum voltage distribution of the ADN is shown in Figure 13.

Looking at Table 2 and Figure 13, compared with method I, the average voltage deviation of method II reduces from 1.7854 p.u. to 1.3219 p.u., and the overall operating losses of method II reduces from 1113.65 kWh to 799.94 kWh, which shows that the use of SOPs is effective in reducing voltage variations and operating losses of ADNs.

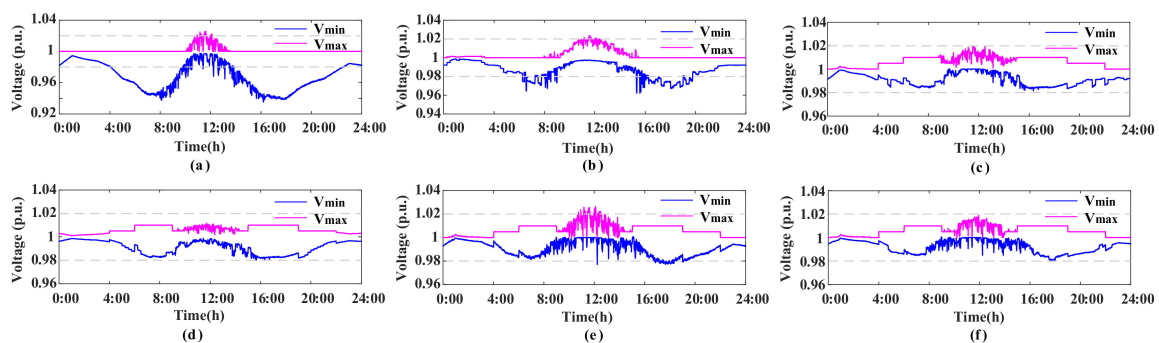
After adding the first stage optimization model of the proposed voltage control method into method II, method III results in lower operating losses and lower average voltage deviation compared to method II. In addition, the voltage variations after control are in the ideal range. These results indicate that the established optimization model of the OLTC and CBs can effectively deal with the uncertainties of the PV outputs and loads. Compared with method III, the active and reactive power are optimized cooperatively in the second stage of the proposed method, and SOPs still have reactive power outputs in the dead zone. Therefore, the operating losses can be significantly reduced.

Both method IV and the proposed voltage control method can control the voltage variations of all nodes within the required voltage range, but the average operating losses of method IV are significantly larger than those of the proposed method. It indicates that optimizing Q-V droop settings according to

the PV outputs and network structure and making full use of SOPs' regulation abilities are helpful in reducing the operating losses of ADNs.

**Table 2.** Comparisons of different voltage regulation methods.

Methods	Overall Operating Losses (kWh)	Minimum Voltage (p.u.)	Maximum Voltage (p.u.)	Average Voltage Deviation (p.u.)
Method I	1113.65	0.9352	1.0260	1.7854
Method II	799.94	0.9567	1.0240	1.3219
Method III	791.46	0.9816	1.0200	1.1485
Method IV	913.06	0.9800	1.0120	1.1088
Method V	594.81	0.9770	1.0260	1.2176
Proposed method	594.98	0.9800	1.0195	1.1588



**Figure 13.** The minimum and maximum voltage based on different control methods: (a) Method I; (b) Method II; (c) Method III; (d) Method IV; (e) Method V; (f) Proposed method.

For method V, the output power of SOPs is optimized every 15 min, thus it cannot effectively mitigate the voltage changes during the control interval. Although method V and the proposed method have almost the same performance in reducing operating losses, the average voltage deviations of method V are larger than those of the method developed in this work. These results show that the real-time Q-V droop control of SOPs plays an important role in regulating real-time voltage fluctuations caused by rapid changes in PV power.

In conclusion, the above comparisons show that the proposed voltage control method can make full use of the voltage regulation capability of SOPs, and the operating losses and voltage fluctuations of ADNs can be remarkably minimized.

## 5. Conclusions

The main goal of the current study was to find a new method to regulate voltage variations using SOPs in ADNs considering uncertainties. A coordinated three-stage voltage regulation method for ADNs is proposed to mitigate nodal voltage fluctuations caused by PV power fluctuations, where the active and reactive power of SOPs, the OLTC tap position, and the reactive power compensation of CBs are optimized in the distribution network level. The main findings are summarized as follows:

(1) The proposed voltage regulation method can not only reduce voltage deviations of all nodes in ADNs, but also can reduce the operating losses.

(2) For a SOP with a certain capacity, the optimization of its active and reactive output power should be considered at the same time, ensuring that the SOP can be fully used to participate in the voltage regulation of ADNs.

(3) When utilizing Q-V droop control algorithm to regulate real-time reactive power of SOPs according to the measured voltage at their connection points, a better voltage regulation result can be obtained if the Q-V droop settings are dynamically optimized in terms of the predicted power of PV plants and loads as well as the topology of ADNs.

(4) In this study, the reactive power corresponding to the dead zone of the Q-V droop curve is periodically optimized, instead of setting the reactive power to zero. Such optimization can not only increase the capability of SOPs in regulating voltage fluctuations, but also can decrease the operating losses of ADNs.

The current study has not been able to consider the coordination between PV plants and SOPs, because this paper mainly aims to investigate the capability of SOPs in controlling voltage variations. Therefore, more researches are required to examine coordinated control methods for SOPs, PV plants, OLTCs, and CBs to suppress nodal voltage fluctuations in ADNs.

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